Hi



























































APL

APL

Ideas

- Precedence rules
- Array oriented
- Concise
- Functions
- Interactive environment

$$10 \div 2 \times 4 + 1 = ?$$

$$10 \div 2 \times 4 + 1 \neq 21$$

$$10 \div (2 \times (4 + 1)) = 1$$

$$10 \div 2 \times 4 + 1 = 1$$



$$1 + 4 = 5$$
 $2 + 5 = 7$
 $3 + 6 = 9$

$$123 + 456 = 579$$

Concise

- Symbols!
- Composition

Symbols!

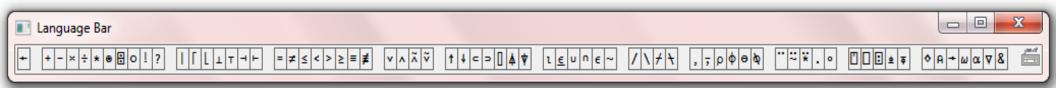
+

_

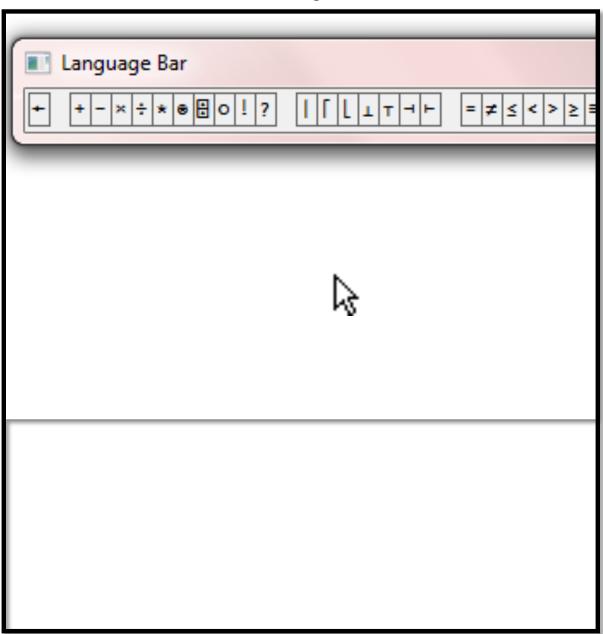
×

÷

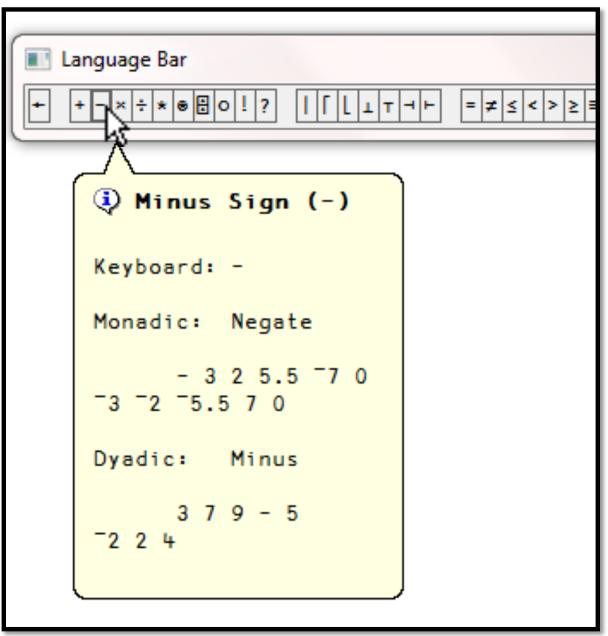
Bonus Feature! -Language Bar-



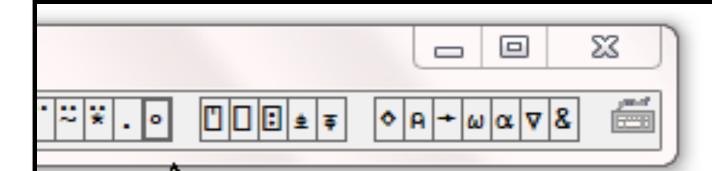
In case of "Symbol Crisis"



In case of "Symbol Crisis"



Composition



Jot (*)

Keyboard: Control+J

Operator: Composed With / Outer Product

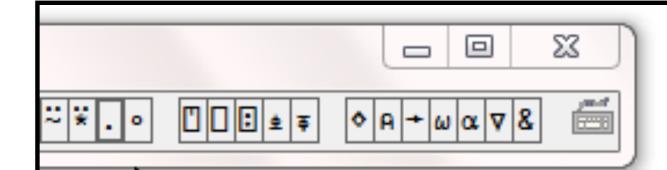
(**0.5) 1 2 3 4 5 6 1 1.414 1.732 2 2.236 2.449

1 2 3 · . × 4 5 6

4 5 6

8 10 12

12 15 18



Inner Product (.)

Keyboard: .

Operator: Inner Product / Outer Product

32

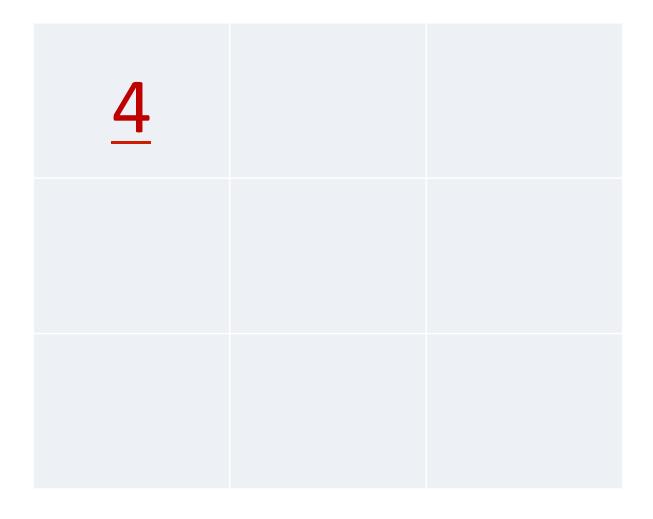
4 5 6

8 10 12

12 15 18

123°.×456

123°.×456



1 2 3 °.× 4 <u>5</u> 6

1 2 3 °.× 4 5 6

1 <u>2</u> 3 °.<u>×</u> <u>4</u> 5 6

4	5	6
8		

1 <u>2</u> 3 °.<u>×</u> 4 <u>5</u> 6

10

1 <u>2</u> 3 °.<u>×</u> 4 5 <u>6</u>

4	5	6
8	10	<u>12</u>

1 2 <u>3</u> °.<u>×</u> <u>4</u> 5 6

4	5	6
8	10	12
<u>12</u>		

1 2 <u>3</u> · .<u>×</u> 4 <u>5</u> 6

4	5	6
8	10	12
12	<u>15</u>	

1 2 <u>3</u> · .<u>×</u> 4 5 <u>6</u>

4	5	6
8	10	12
12	15	<u>18</u>

123°.×456

4	5	6
8	10	12
12	15	18

123°.×456

4	5	6
8	10	12
12	15	18

1 2 3 °.+ 4 5 6

<u>1</u> 2 3 °.<u>+</u> <u>4</u> 5 6

<u>1</u> 2 3 °.<u>+</u> 4 <u>5</u> 6

<u>1</u> 2 3 °.<u>+</u> 4 5 <u>6</u>

5	6	<u>7</u>

1 <u>2</u> 3 °.<u>+</u> <u>4</u> 5 6

5	6	7
<u>6</u>		

1 <u>2</u> 3 °.<u>+</u> 4 <u>5</u> 6

5	6	7
6	<u>7</u>	

1 <u>2</u> 3 °.<u>+</u> 4 5 <u>6</u>

5	6	7
6	7	<u>8</u>

1 2 3 °.+ 4 5 6

5	6	7
6	7	8
<u>7</u>		

1 2 <u>3</u> · .<u>+</u> 4 <u>5</u> 6

5	6	7
6	7	8
7	8	

1 2 <u>3</u> · .<u>+</u> 4 5 <u>6</u>

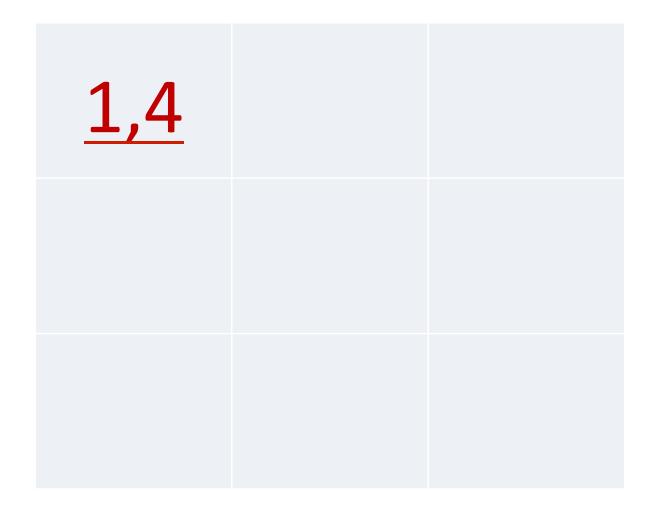
5	6	7
6	7	8
7	8	9

1 2 3 °.+ 4 5 6

5	6	7
6	7	8
7	8	9

123 °., 456

<u>1</u> 2 3 °., <u>4</u> 5 6



2 3 °., 4 **5** 6

<u>1</u> 2 3 °., 4 5 <u>6</u>

1,4	1,5	<u>1,6</u>

1 <u>2</u> 3 °., <u>4</u> 5 6

1,4	1,5	1,6
<u>2,4</u>		

1 <u>2</u> 3 °., 4 <u>5</u> 6

1,4	1,5	1,6
2,4	<u>2,5</u>	

1 <u>2</u> 3 °., 4 5 <u>6</u>

1,4	1,5	1,6
2,4	2,5	2,6

1 2 <u>3</u> °., <u>4</u> 5 6

1,4	1,5	1,6
2,4	2,5	2,6
<u>3,4</u>		

1 2 <u>3</u> °., 4 <u>5</u> 6

1,4	1,5	1,6
2,4	2,5	2,6
3,4	<u>3,5</u>	

1 2 <u>3</u> °., 4 5 <u>6</u>

1,4	1,5	1,6
2,4	2,5	2,6
3,4	3,5	<u>3,6</u>

123 °., 456

1,4	1,5	1,6
2,4	2,5	2,6
3,4	3,5	3,6

$123 + \times 456$

 $123 + \times 456$

4

10

<u>18</u>

$$123 + \times 456$$

Anonymous functions

$$2 = 10 \div 5$$

$$2 = 10 \{\alpha \div \omega\} 5$$

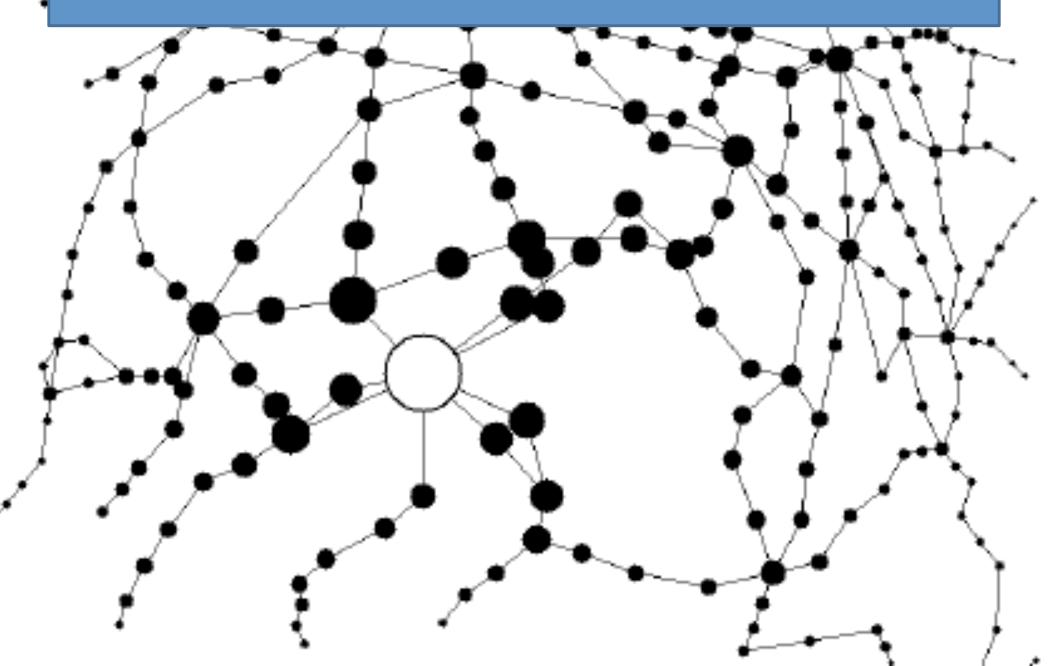
$$14 = 10 \{\alpha + (8 \times (\omega \div \alpha))\} 5$$

Assignment

DividedBy $\leftarrow \{\alpha \div \omega\}$



I wonder...



Flights

To LAX OAK **SFO** SAN LAX **SFO** SAN **OAK**

From

OneHop—Flights

	IO				
		LAX	SFO	SAN	OAK
	LAX	0	1	0	0
	SFO	1	0	1	0
•	SAN	0	1	0	0
	OAK	0	0	1	0

rom

TwoHops ←OneHop +.× OneHop

		LAX	SFO	SAN	OAK	
	LAX	1	0	1	0	
-	SFO	0	2	0	0	
	SAN	1	0	1	0	
	OAK	0	1	0	0	

rom

ThreeHops←OneHop +.× TwoHops

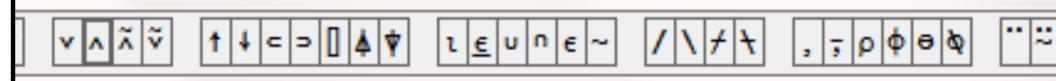
	I O				
		LAX	SFO	SAN	OAK
	LAX	0	2	0	0
	SFO	2	0	2	0
•	SAN	0	2	0	0
	OAK	1	0	1	0

rom

AllTrips←OneHop + TwoHops + ThreeHops

	LAX	SFO	SAN	OAK	
LAX	1	3	1	0	
SFO	3	2	3	0	
SAN	1	3	1	0	
OAK	1	1	2	0	

-rom



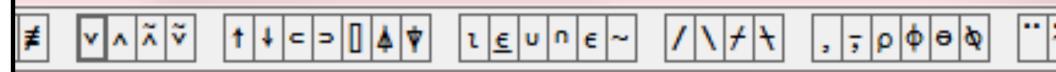
Logical And (^)

Keyboard: Control+0

Dyadic: Logical And / Lowest Common Multiple

0 1 0 1 ^ 0 0 1 1

15 1 2 7 ^ 35 1 4 0 105 1 4 0



Logical Or (v)

Keyboard: Control+9

Dyadic: Logical Or / Greatest Common Divisor

0 1 0 1 v 0 0 1 1 0 1 1 1

15 1 2 7 v 35 1 4 0

5 1 2 7





TwoHops ← OneHop +.× OneHop

	IO				
		LAX	SFO	SAN	OAK
	LAX	1	0	1	0
	SFO	0	2	0	0
•	SAN	1	0	1	0
	OAK	0	1	0	0

TwoHops ← OneHop V.∧ OneHop

	LAX	SFO	SAN	OAK
LAX	1	0	1	0
SFO	0	1	0	0
SAN	1	0	1	0
OAK	0	1	0	0

ThreeHops←OneHop V.∧ TwoHops

	IO				
		LAX	SFO	SAN	OAK
	LAX	0	1	0	0
	SFO	1	0	1	0
•	SAN	0	1	0	0
	OAK	1	0	1	0

AllTrips←OneHop V TwoHops V ThreeHops

	IO				
		LAX	SFO	SAN	OAK
	LAX	1	1	1	0
	SFO	1	1	1	0
•	SAN	1	1	1	0
	OAK	1	1	1	0

ThreeHops←OneHop ∨ OneHop ∨ . ∧ TwoHops

NextHops←PrevHops V PrevHops V.∧ ThisHops

NextHops \leftarrow PrevHops $\{\alpha \lor \alpha \lor . \land \omega\}$ ThisHops

③ DieresisStar (*)

Keyboard: Control+Shift+P

Operator: Power

(↓*1) 2 2 2 2 p□a A split once.

AB CD

EF GH

IJ KL

MN OP

(↓¥2) 2 2 2 2p∏a A split twice.

AB CD EF GH

IJ KL MN OP

(↓¥3) 2 2 2 2p□a A split thrice

AB CD EF GH IJ KL MN OP

f+(32∘+)∘(×∘1.8) A Fahrenheit from Celsius

f ⁻273 ⁻40 0 100

-459.4 -40 32 212

c+f^{*−}1 A Inverse: Celsius from Fahrenheit

c ~459.4 ~40 32 212

-273 -40 0 100

ThreeHops←OneHop ∨ OneHop ∨ . ∧ TwoHops

NextHops←PrevHops ∨ PrevHops ∨ . ∧ ThisHops

NextHops \leftarrow PrevHops $\{\alpha \lor \alpha \lor . \land \omega\}$ ThisHops

AllTrips \leftarrow OneHop ({ $\alpha \lor \alpha \lor . \land \omega$ } *3) OneHop

AllTrips \leftarrow OneHop ($\{\alpha \lor \alpha \lor . \land \omega\} * \equiv$) OneHop

AllTripsFor $\leftarrow \{\omega \ (\{\alpha \ \lor \alpha \ \lor . \land \omega\} \ \times \ \equiv) \ \omega\}$

AllTripsFor
$$\leftarrow \{\omega \ (\{\alpha \ \lor \alpha \ \lor . \land \omega\} \ * \equiv) \ \omega\}$$

$$Or \leftarrow V$$

ConnectedTo $\leftarrow V.\Lambda$

UntilNoChange $\leftarrow \{\alpha \ \alpha\alpha \ \ast \equiv \omega\}$

AppliedTo $\leftarrow \{\omega \ \alpha\alpha \ \omega\}$

AllTripsFor \leftarrow ({ α Or α ConnectedTo ω } UntilNoChange) AppliedTo

AllTripsFor Flights

What I covered

- Precedence rules
- Array oriented
- Concise
- Functions
- Interactive environment

Things you didn't see

- Memory allocation
- For loops
- A source file
- Types



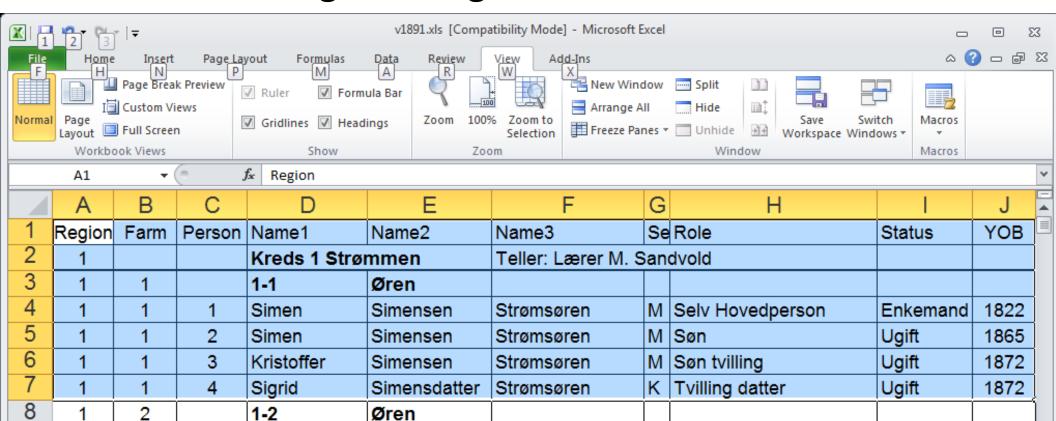
Joel@JoelHough.com

The old guy with no hat ...

- Morten Kromberg, CTO of Dyalog Ltd.
 - Dyalog is the leader of the [still] emerging APL Market ☺
 - Basingstoke (UK) + Canada, DK, France, USA
- 1 year Z80, 1 year Commodore BASIC, 33 yrs APL
 - IBM 5100 APL, SHARP APL, IBM VSAPL and APLSV,
 DEC APL/SF, MIPS APL (Prime), Data General APL,
 IBM APL2, APL*PLUS/PC, APL+Win, and now Dyalog APL
- Wrote at least one program that I understood in each of:
 - 6502 and Z80 Machine code, JCL
 - Simula, Pascal, COBOL, C, C#, Java
- ... (Plus one program in Prolog)
- CTO of Adaytum, BI "startup" based on APL
 - Sold to Cognos in 2000 for \$160M

Interactive Demo

- A Day in the Life of a Domain Expert
 - Domain: History
- Build a DSL for Playing with Tables
- Do something that might be hard in SQL



What I Hope to Show You...

- That APL is an inherently parallel notation which makes it easy to think about, and "crunch", arrays
- That APL encourages the construction of functional DSL's – without demanding a purely functional approach to coding
- That APL is a "tool of thought", which helps us discover suitable algorithms and solutions through experimentation

What I Hope I Demonstrated...

- The Data is at your Fingertips™
- APL Encourages the construction of functional DSLs
 - Work closely with or BE the Domain Expert
- ... That Dyalog APL blends Array, Functional and Object Oriented paradigms "seamlessly"
 - Allows you to use the Tool of Thought which is appropriate to the task
- ... with tight interop with Object Frameworks
 - Provide, Consume and Extend COM, CLR (& soon JVM)
 Classes

Parallelism

- "Map" is the default behaviour for many primitives
- We automagically parallelize each function in

+/ Quantity × Price ÷ Discount

- IBM APL2 used the "370 Vector Facility" from 1987
- However, on modern hardware, "interpreted SIMD" hits memory bottlenecks hard

Parallelism ...

- We are working on a compiler and considering "optional type declarations", etc.
- Many "idioms" are already recognized by the interpreter. For example $X/\iota \rho X$.
- We have an experimental interpreter w/closures
- P.Each P.Outer P.Rank are multi-process versions of familiar APL "operators"
 - Refactoring can be handled by non-technical developers
 - Insurance company saw 5x speedup on 8-core i7 for pension calculations
 - "bang for the buck" here and now

Can an interpreter be FAST?

- You can always write a faster program in a compiled language...
 - IF you have the time to figure out how to do it right
 - On large data, APL expressions have VERY LITTLE interpreter overhead very few loops
 - $(+/\omega + \rho\omega)$ can be thought of as "bytecode"
 - We have spent 30 years optimizing 1-bit, 1-, 2- and 4byte integers, so arrays are compact
 - ... and memory access is getting expensive
 - Some parallelism is automatic

In Practice ...

- On synthetic benchmarks, C[#]&family usually beat APL
- ... But large APL applications often outperform and "outscale" competitors using compiled languages
- Close collaboration between domain experts and software engineers allows efficient operations on compact data representations
 - In rare cases hotspots are recoded in C & friends after "discovery" in APL (APL code lives on for R&D and QA)
- It is straightforward to experiment and discover alternative algorithms, and apply mathematical insights
- Object hierarchies seem to encapsulate data in ways which severely constrain the set of possible optimizations

Types and Correctness

- APL is called "write only" by those who can not read it, in practice the reverse is true for well-written code
 - Compare $\{+/\omega \div \rho \omega\}$ to traditional alternatives
- No type definitions, almost no loops or other "fluff"
- Extremely high "semantic density" leads to Domain Experts being able to read the code and participate in refactoring
- Build in hours, refactor & ship frequently for decades ©
- The really interesting bug is the broken algorithm

"The only program that stands a chance of being correct is a short one."

(Arthur Whitney, Kx Systems)

Some Customers

- SimCorp (DK), APL Italiana (I),
 Fiserv Investment Services (US), Infostroy Ltd (Russia)
 - Leaders in various markets for Asset Management Systems
- KCI Corp (US)
 - Budgeting and Planning
- Carlisle Group (US)
 - Collateral and Securitization for Global Capital Markets
- ProfDoc Care (Sweden)
 - One of the worlds largest Patient Journal systems with 40,000 users and
 2.5 million patient records in Sweden, and sub-second response
- ExxonMobil (US)
 - Optimizes the "Cracking" of Petroleum Products using APL
- Typically used in emerging or constantly churning markets

Curious?

- Download free "Mastering Dyalog APL" PDF (or buy hardcopy from Amazon)
- Download a Free Trial System
 - Windows 32-bit,
 Contact Dyalog for trials on other platforms

→ HTTP://TRYAPL.ORG